

# SAR Calibration Requirements for Interferometry Applications: inching towards sub millimeter measurements

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# WHY ?

Requisites for CO<sub>2</sub> storage and oil  
reservoirs monitoring  
(30% of the energy right away,  
10000 years sequestration ???)

Reservoir kinematics  
From Volume Changes to Surface Deformation

A one line theory



## From elasticity theory

In the case of an elastic model, starting from Segall (1985), it's possible to get the relation between surface deformation and percentage volume change. The vertical deformation is:

$$u_z(x, y, z) = \int_V \Delta(\bar{\xi}) g_z(x, y, z, \bar{\xi}) dV$$

where  $\bar{\xi} = (\xi_1, \xi_2, \xi_3)$  ranges over  $V$

$$g_z(x, y, z, \bar{\xi}) = \frac{(1 + \nu)}{3\pi} \frac{z - \xi_3}{\left( \sqrt{(x - \xi_1)^2 + (y - \xi_2)^2 + (z - \xi_3)^2} \right)^3}$$



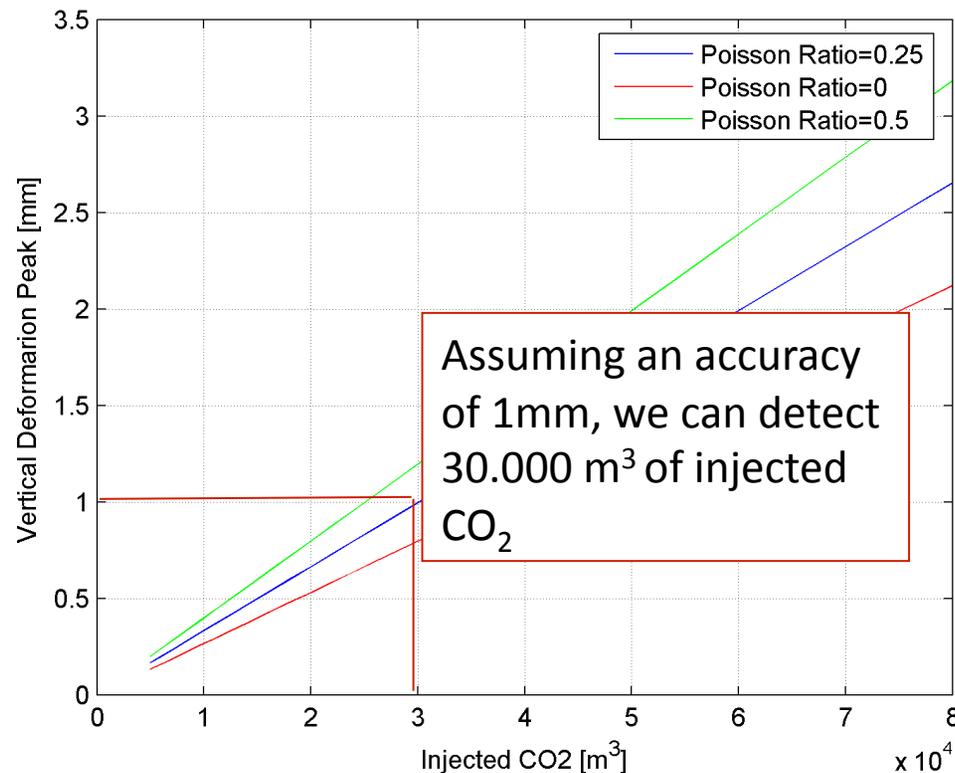
$\nu$  is the Poisson Ratio ( $0 < \nu < 0.5$ )

## In case of $CO_2$ injection

- What's the minimum amount of injected  $CO_2$  we can detect using PSInSAR™?

Assuming:

- a reservoir **2Km** depth
- a **single layer** overburden



# InSalah Case study (Algeria)

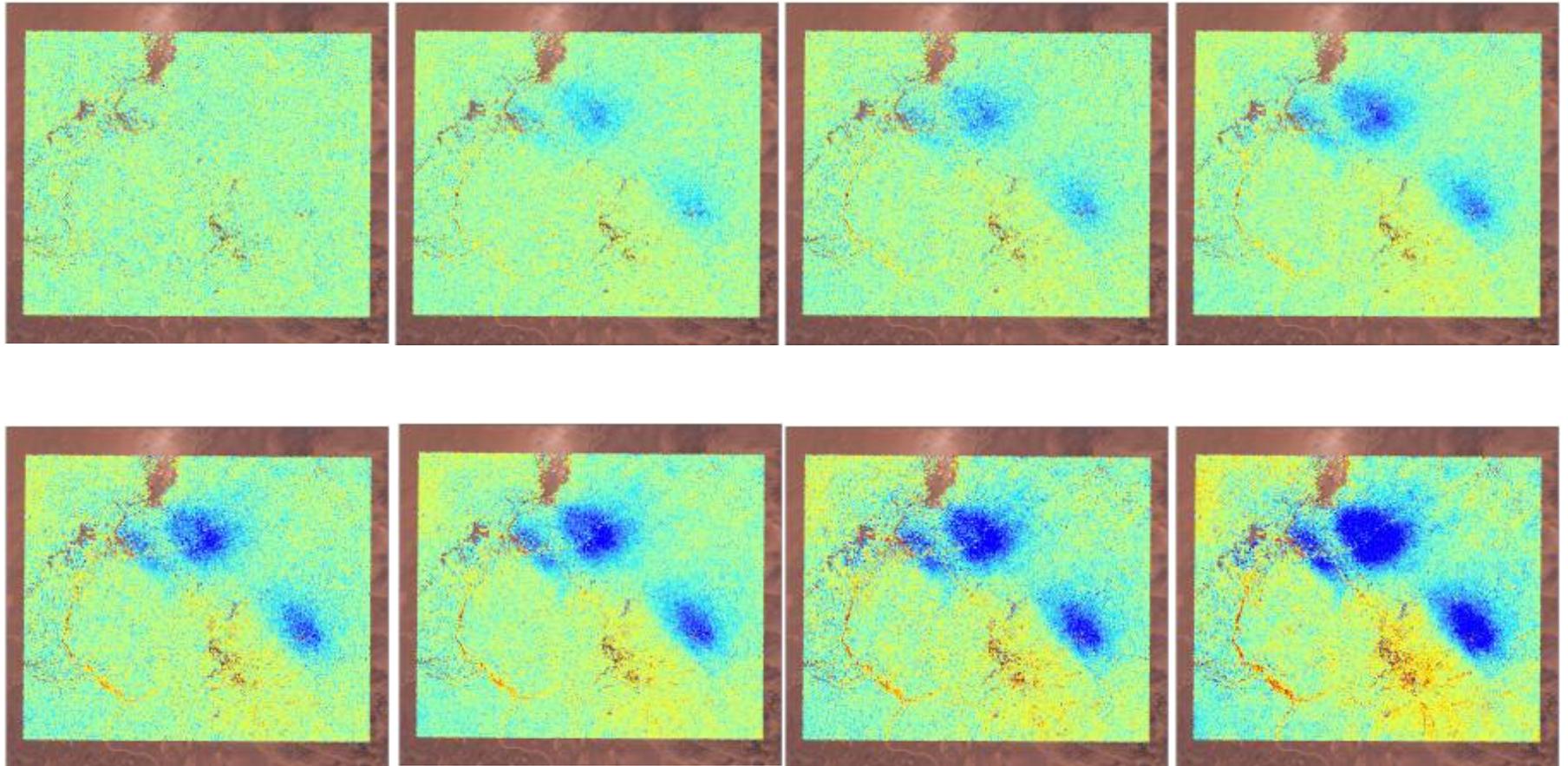
The InSalah Gas storage project is the first  $\text{CO}_2$  sequestration effort in an active reservoir.

1 million  $\text{CO}_2$  tons are reinjected into the subsurface each year.

PSInSAR estimated volume and pressure changes, and finally the permeability within the reservoir. A fault had been reactivated.



# CO2 Sequestration - North Africa



Pattern anisotropy → Fault reactivation?





# Arrival time and Trajectories

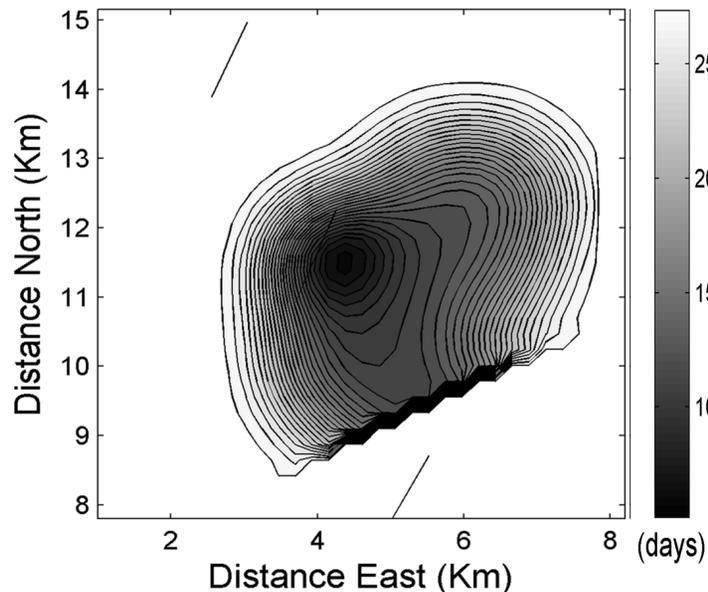
Pressure changes → propagating fronts

We use the time derivative of the pressure

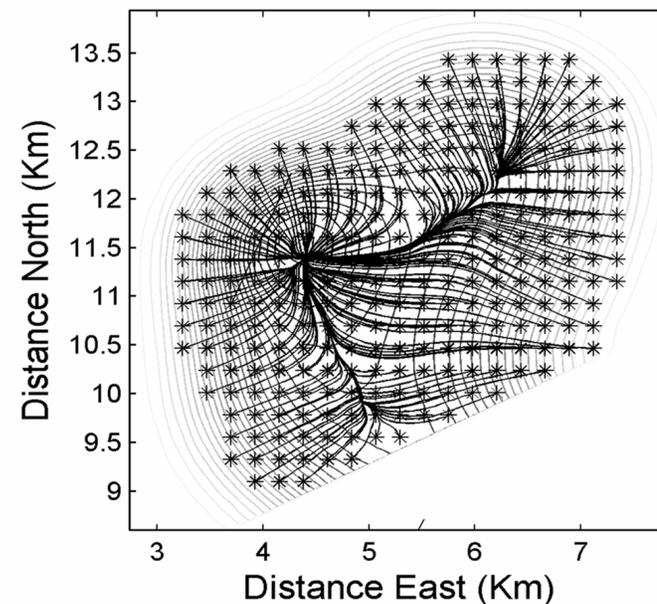
From the time arrivals → permeability

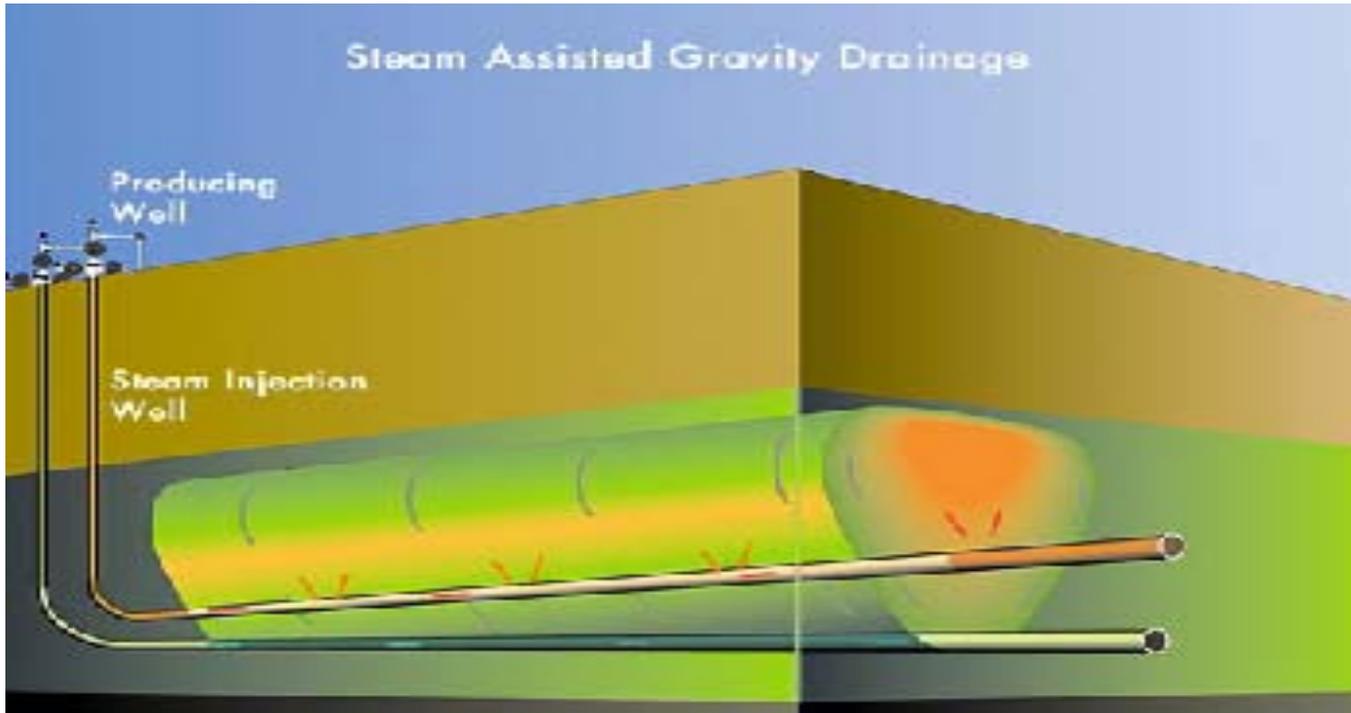
A. Rucci, D. W. Vasco, Fluid pressure arrival time tomography, SEG 2009, Houston

Arrival time



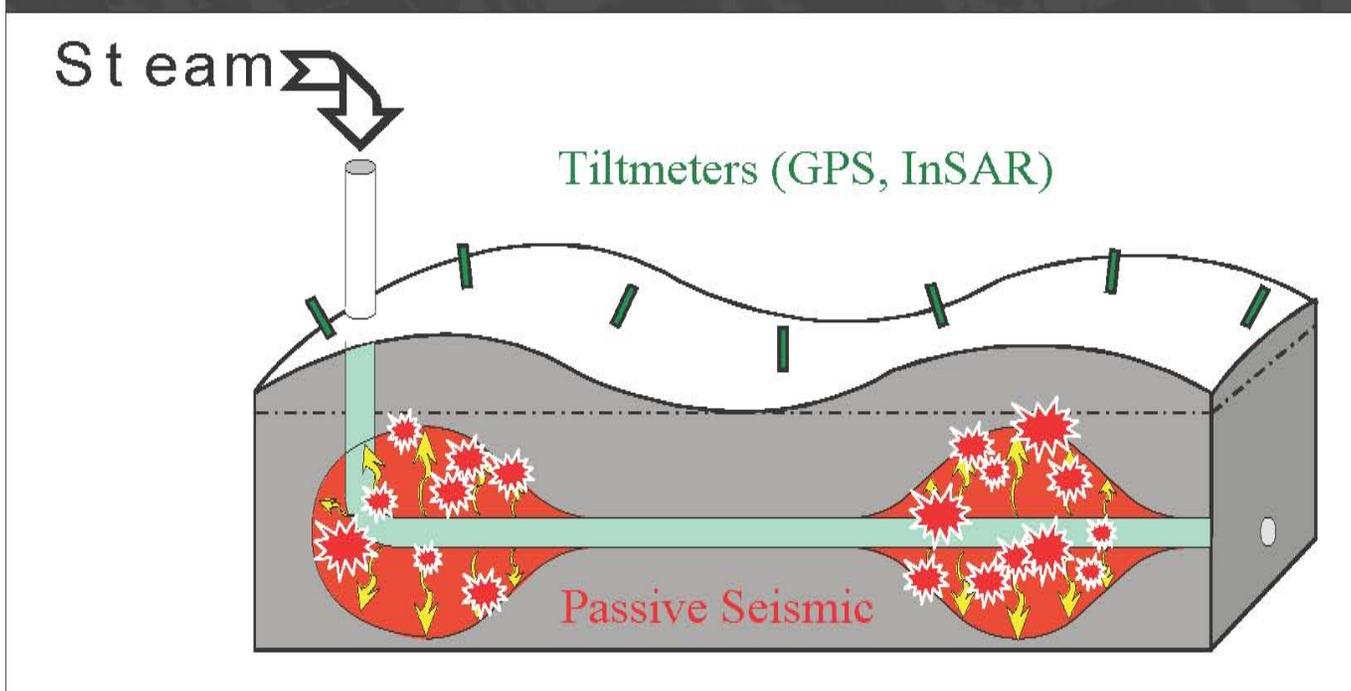
Trajectories

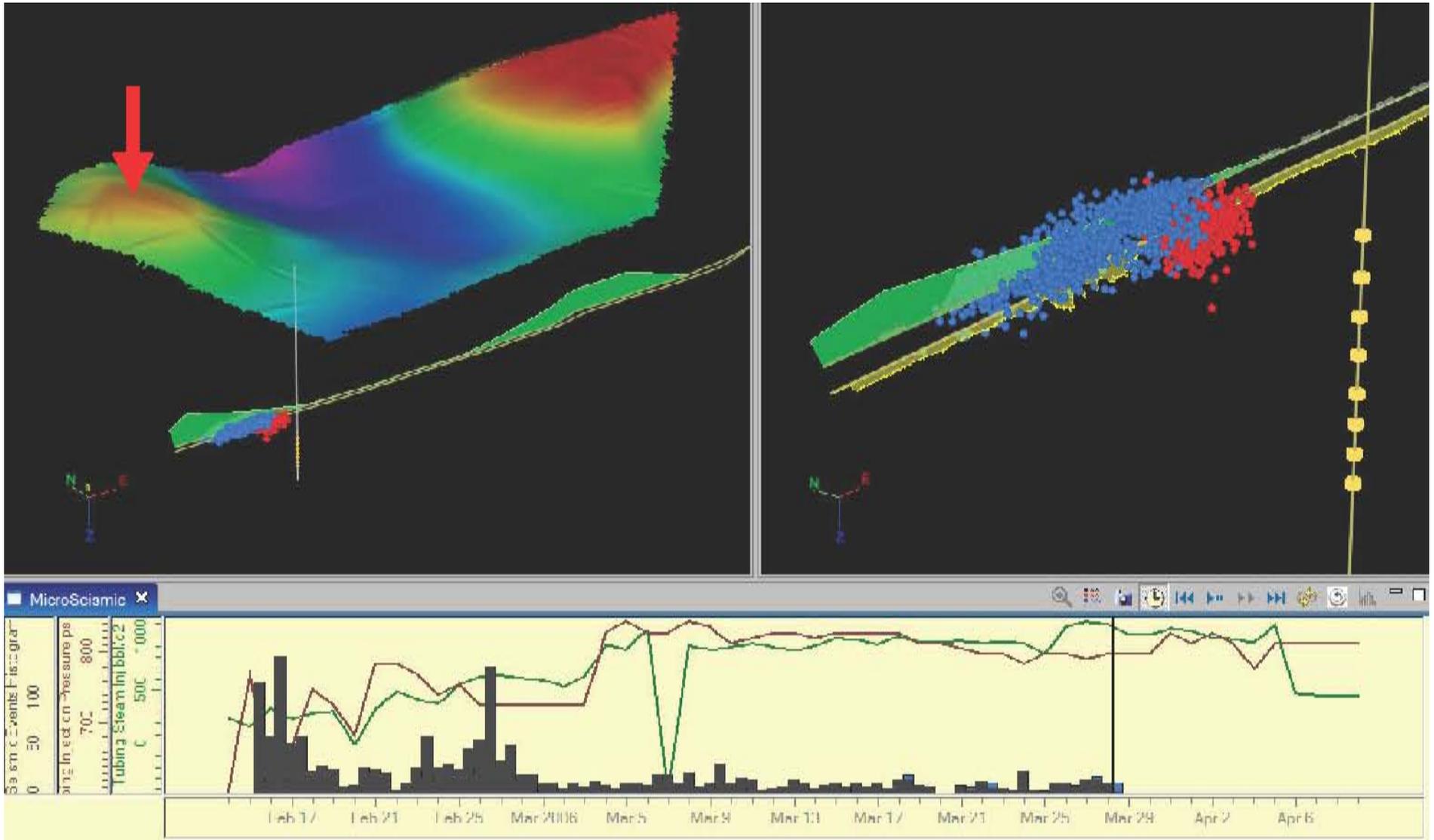




Steam Assisted Gravity Drainage

Heavy crudes





**Microseismics precede subsidence**



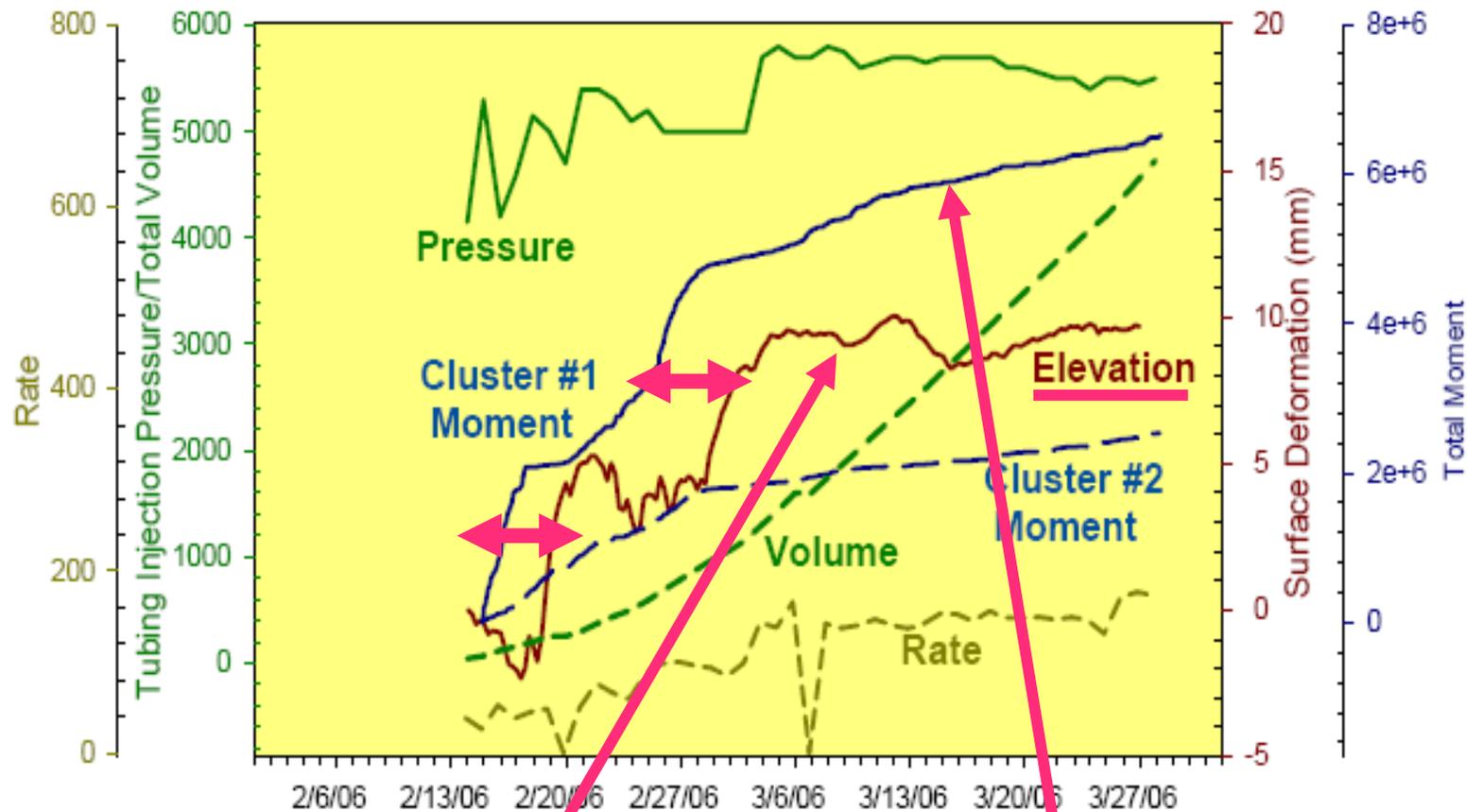


Figure 5. Time line of the injection, seismic deformation and elevation change.

The periods of significant seismic release precede periods of uplift by a few days. The microseismic data shows the creation of a fracture network to be later filled with steam causing the surface uplift.



We can map surface deformations into permeability changes and fault patterns; the InSalah story is condensed in 1 cm surface motion

1 mm sensitivity is achieved today with reduced resolution, but can improve with numerical atmospheric models.

The revisit time is paramount



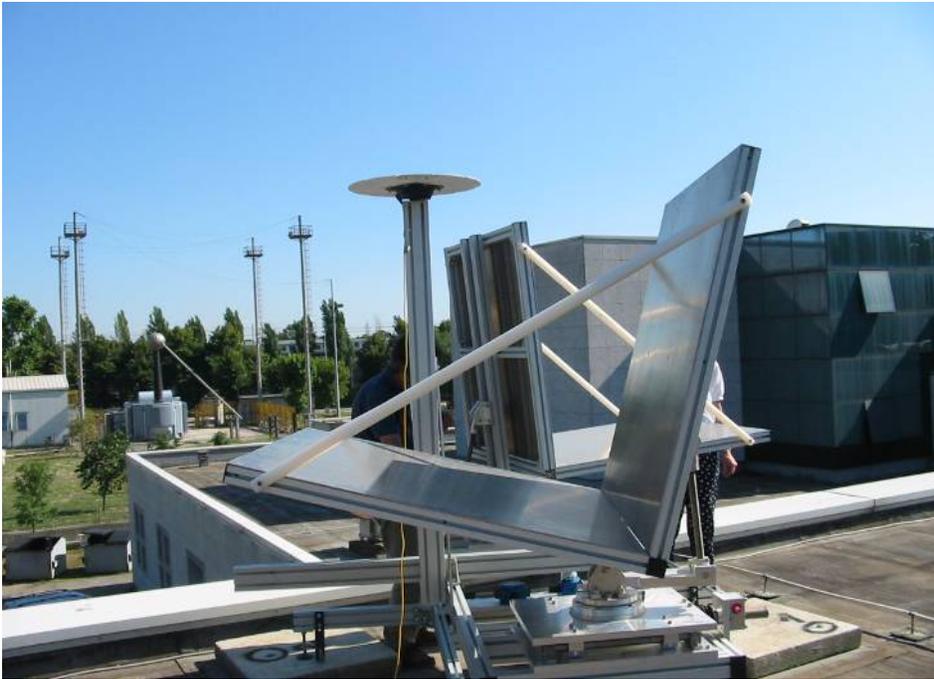
# HOW ?

What we can do today with  
good atmospheric control  
i.e. with  
a dense and long set of PS



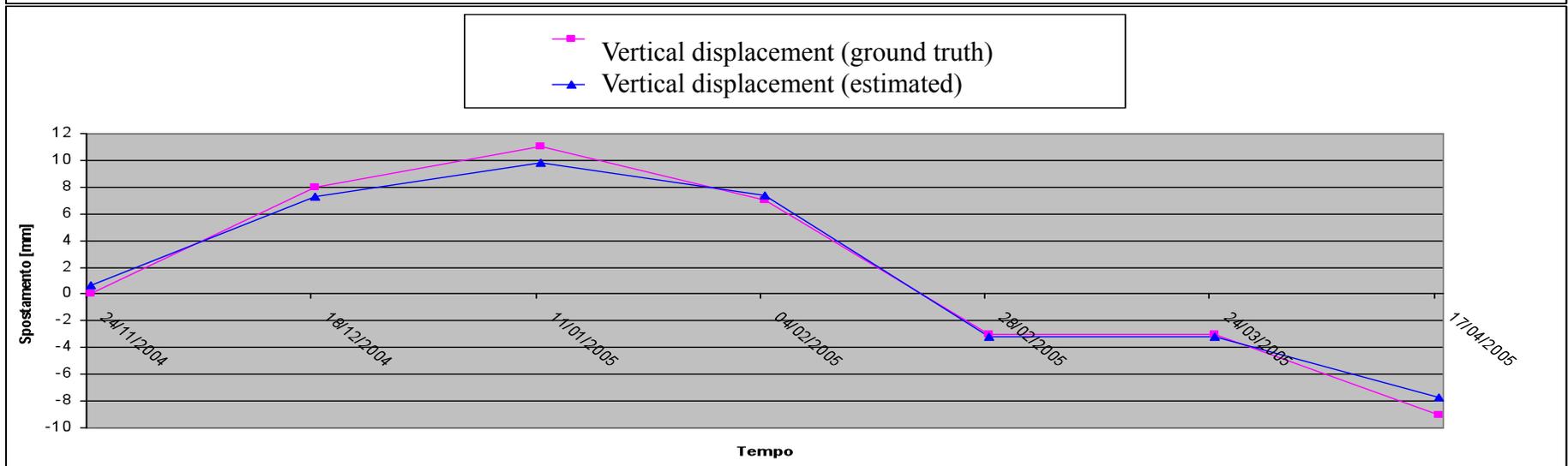
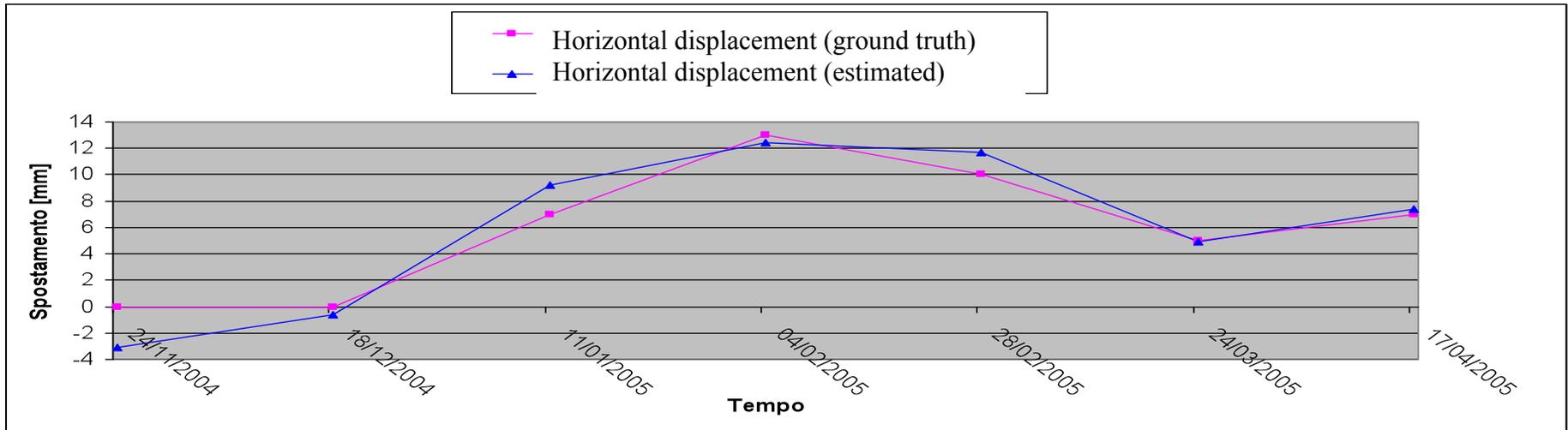
# The CESI experiment

## Ground Based Radars: The XX dam



# The CESI experiment

## Estimated displacement (Radarsat 1 data)



Rmse = 0.58mm (h!); 0.75mm (v)



# A Ground Based SAR at the XX dam

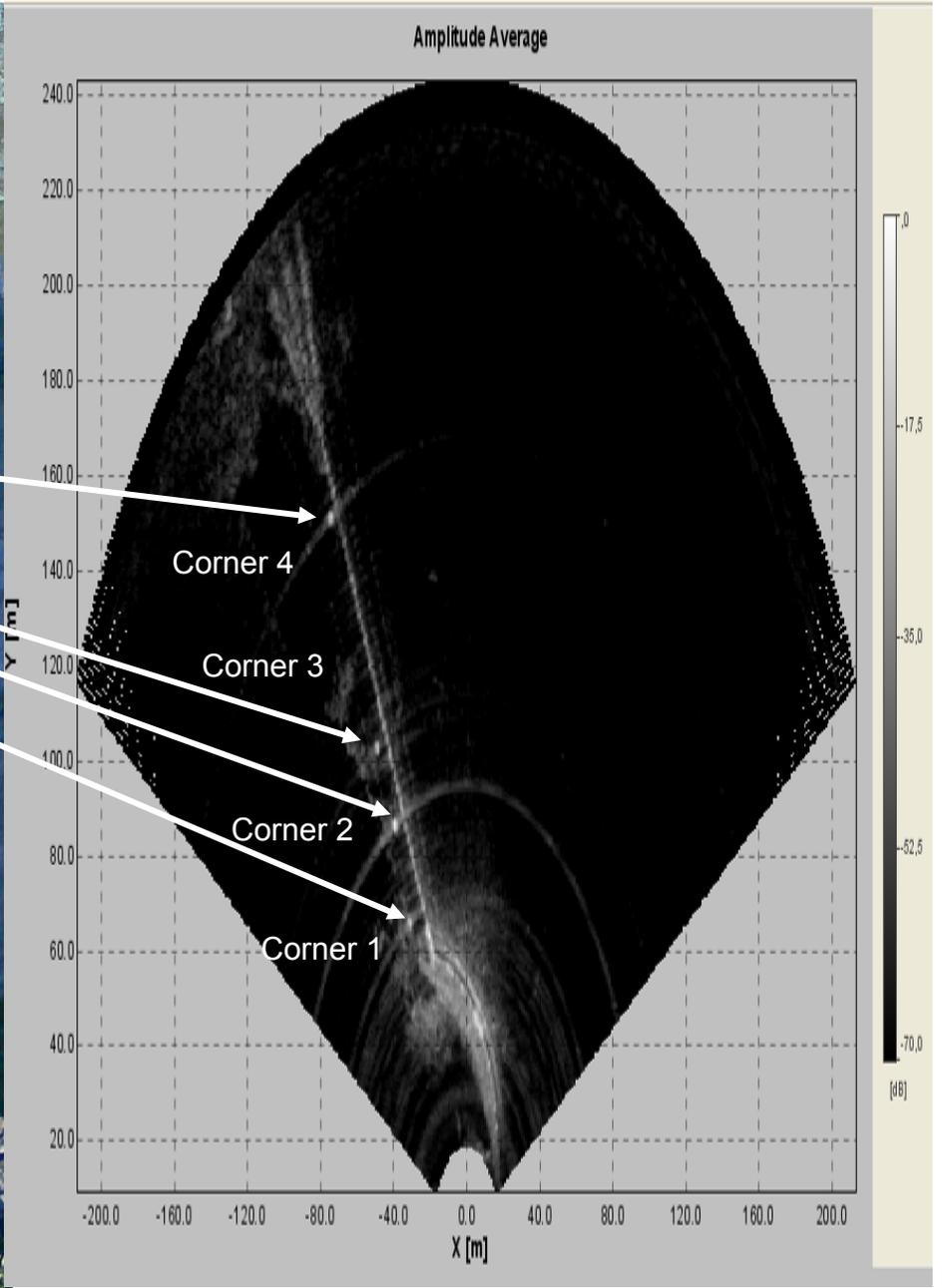
Contribution by D. Giudici, Aresys



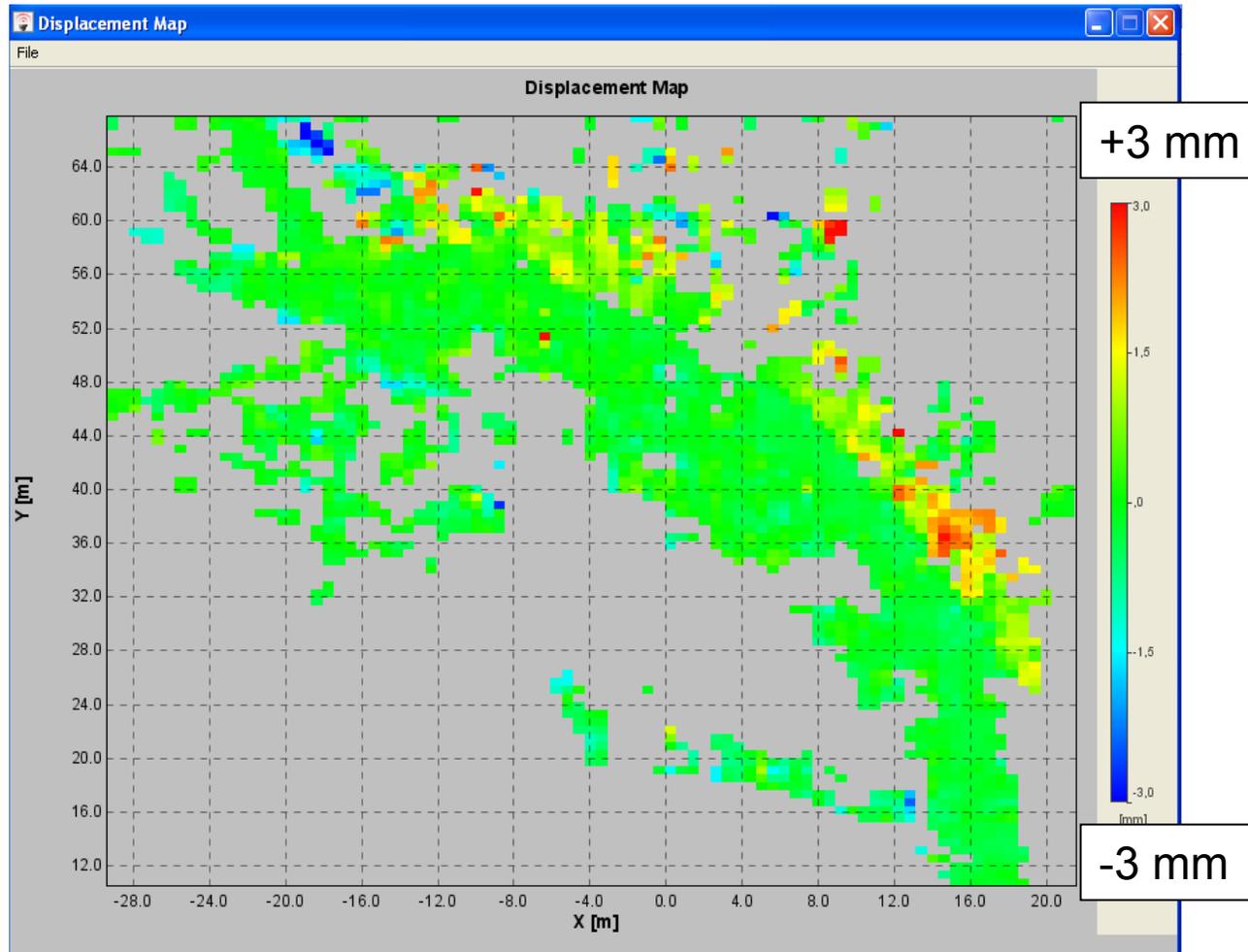
IBIS-L



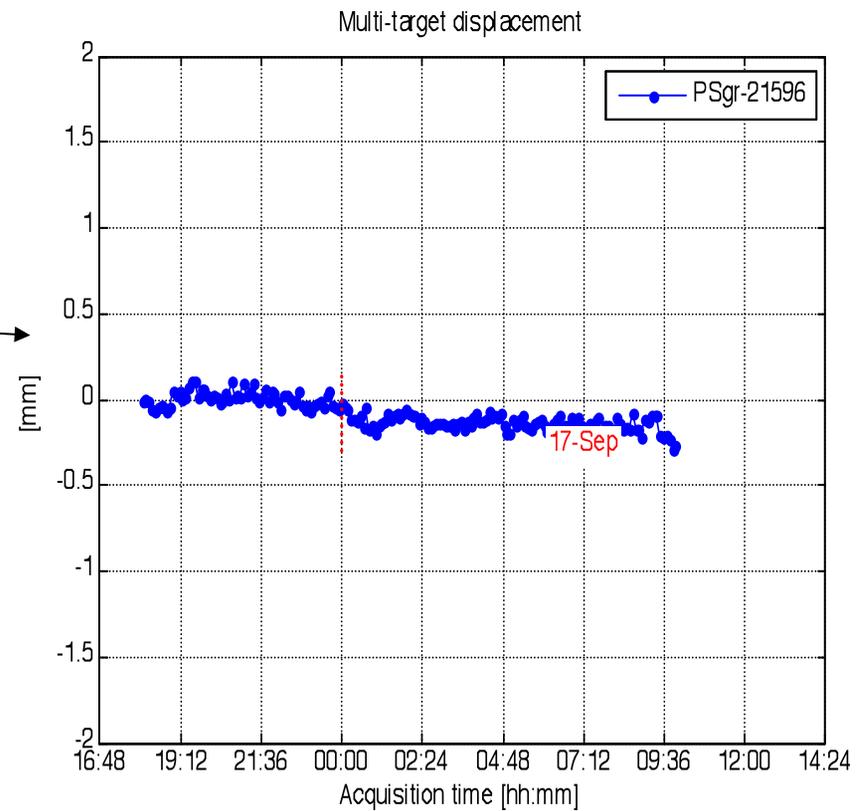
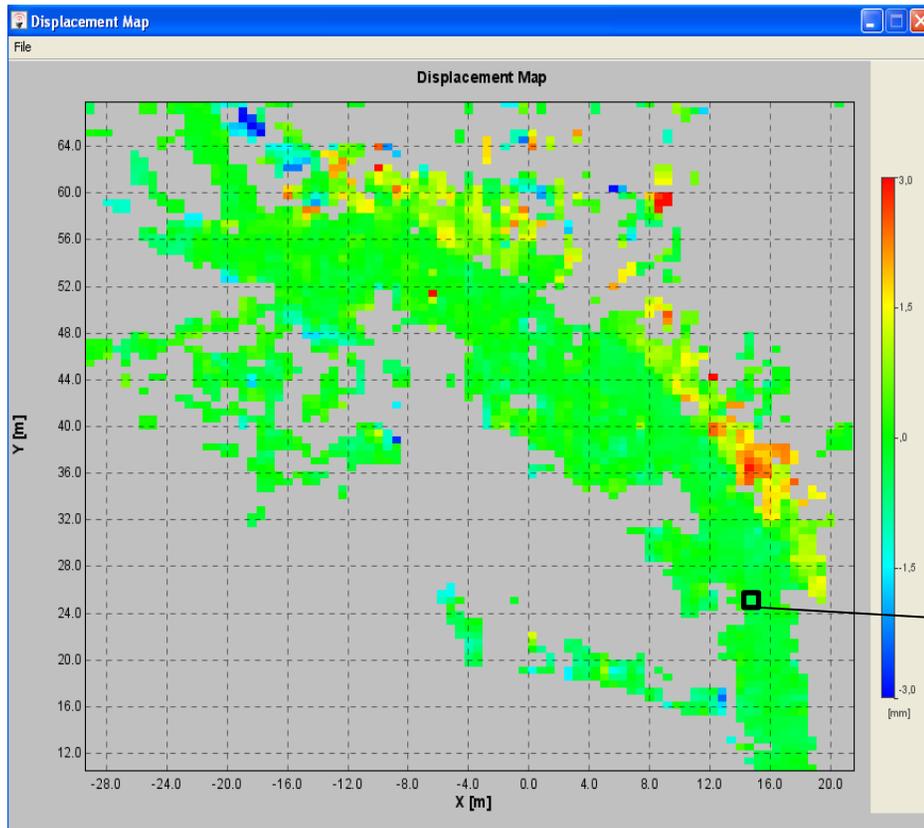
The future: UAV, geosynchronous, both?



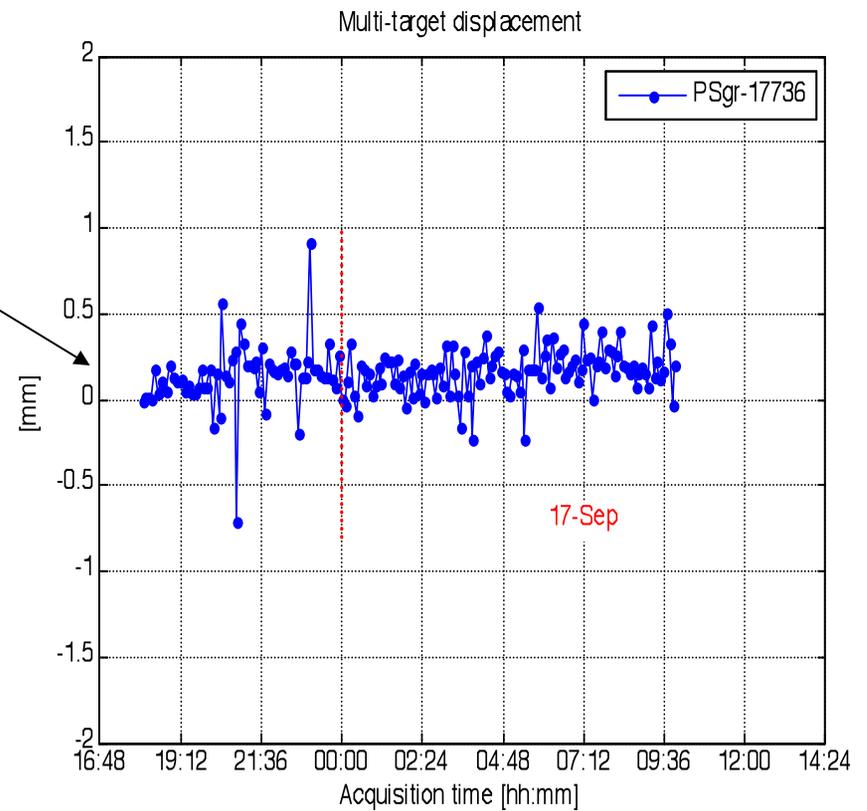
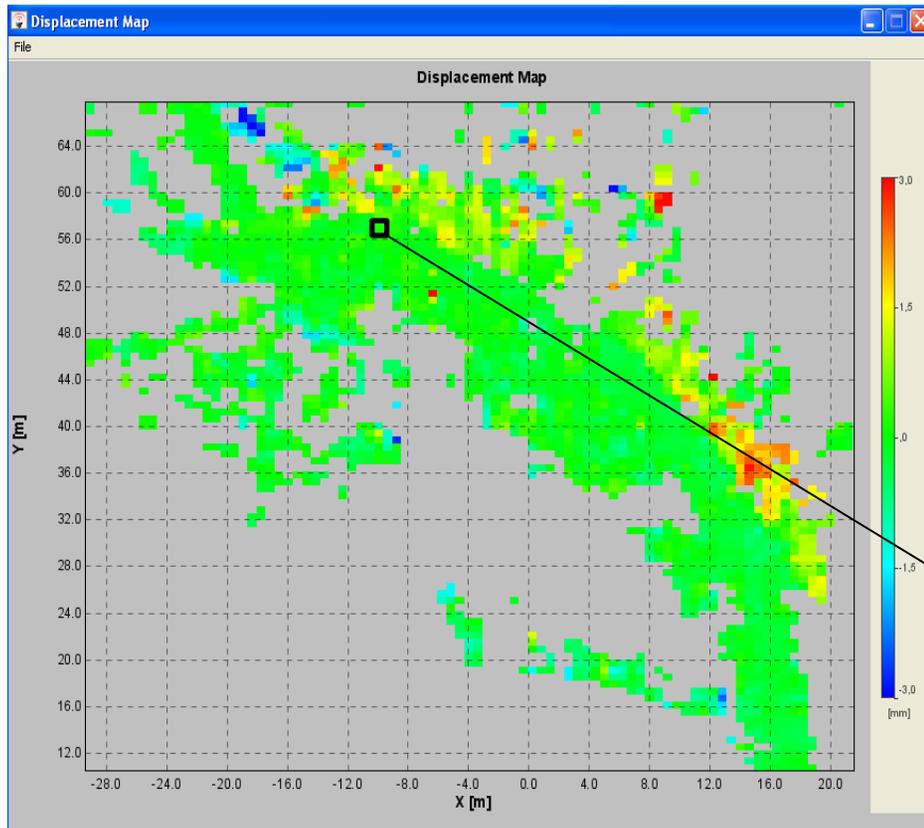
# Permanent Scatterers displacement analysis: close view



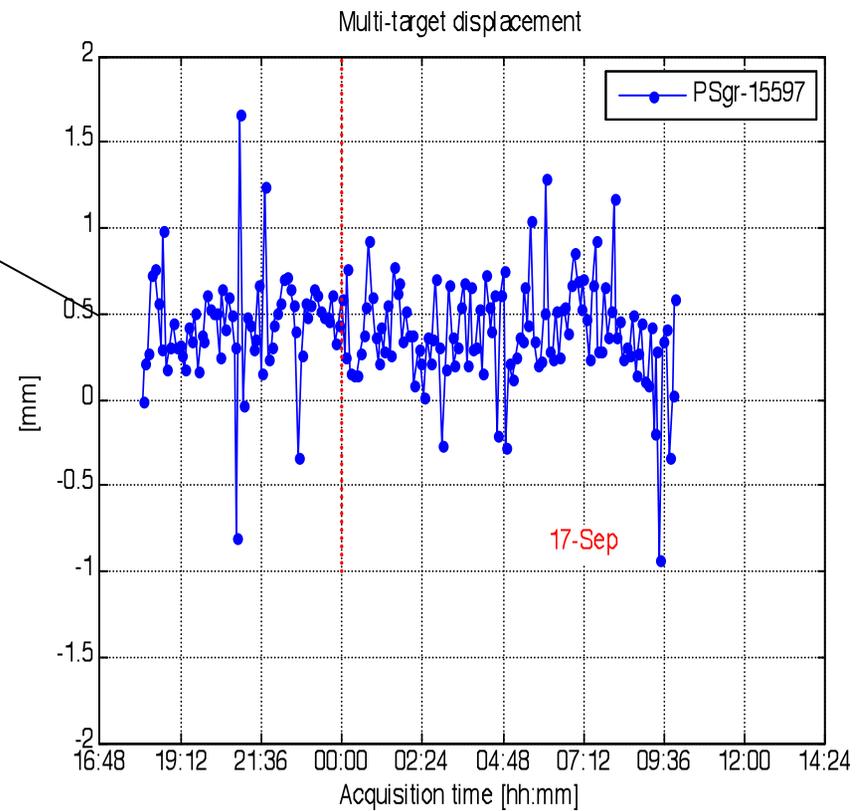
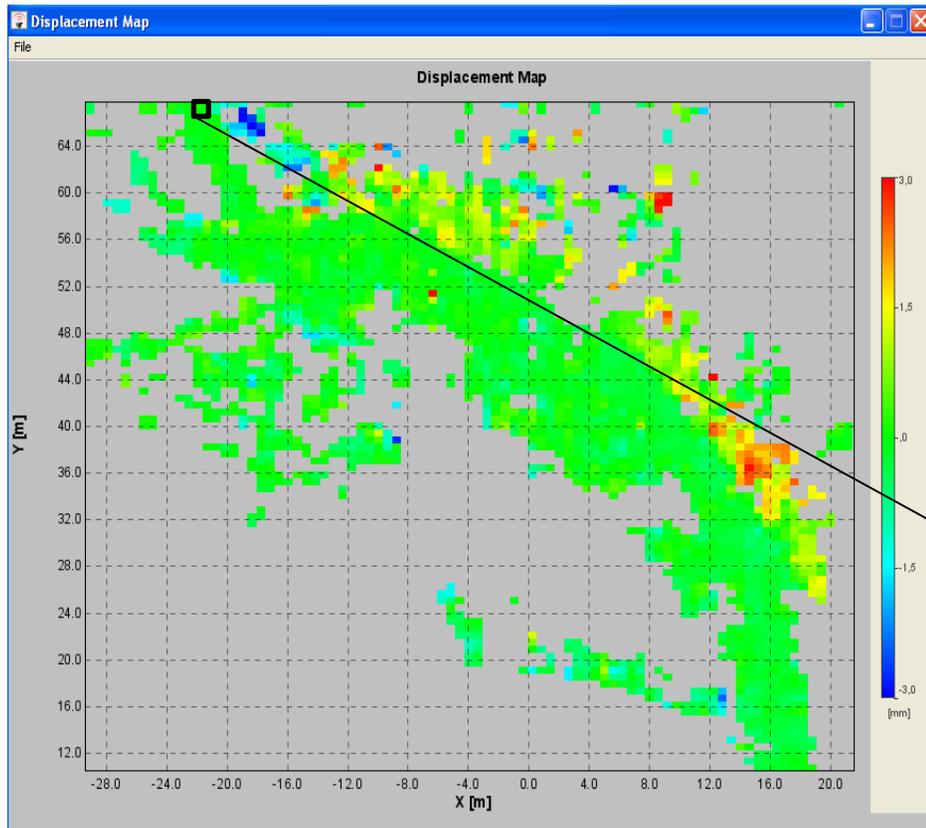
# Permanent Scatterers analysis : displacement series



# Permanent Scatterers analysis : displacement series



# Permanent Scatterers analysis : displacement series



# Conclusions for the Ground Based SAR (15 h. observation)

The data show coherence  $> 0.8$

The atmospheric effect is very low for the good meteorological conditions

The rms noise is of the order of **0.1mm**



# HOW !



Controlling the  
Atmospheric Phase Screen  
from the satellite  
with a dense and long set of PS

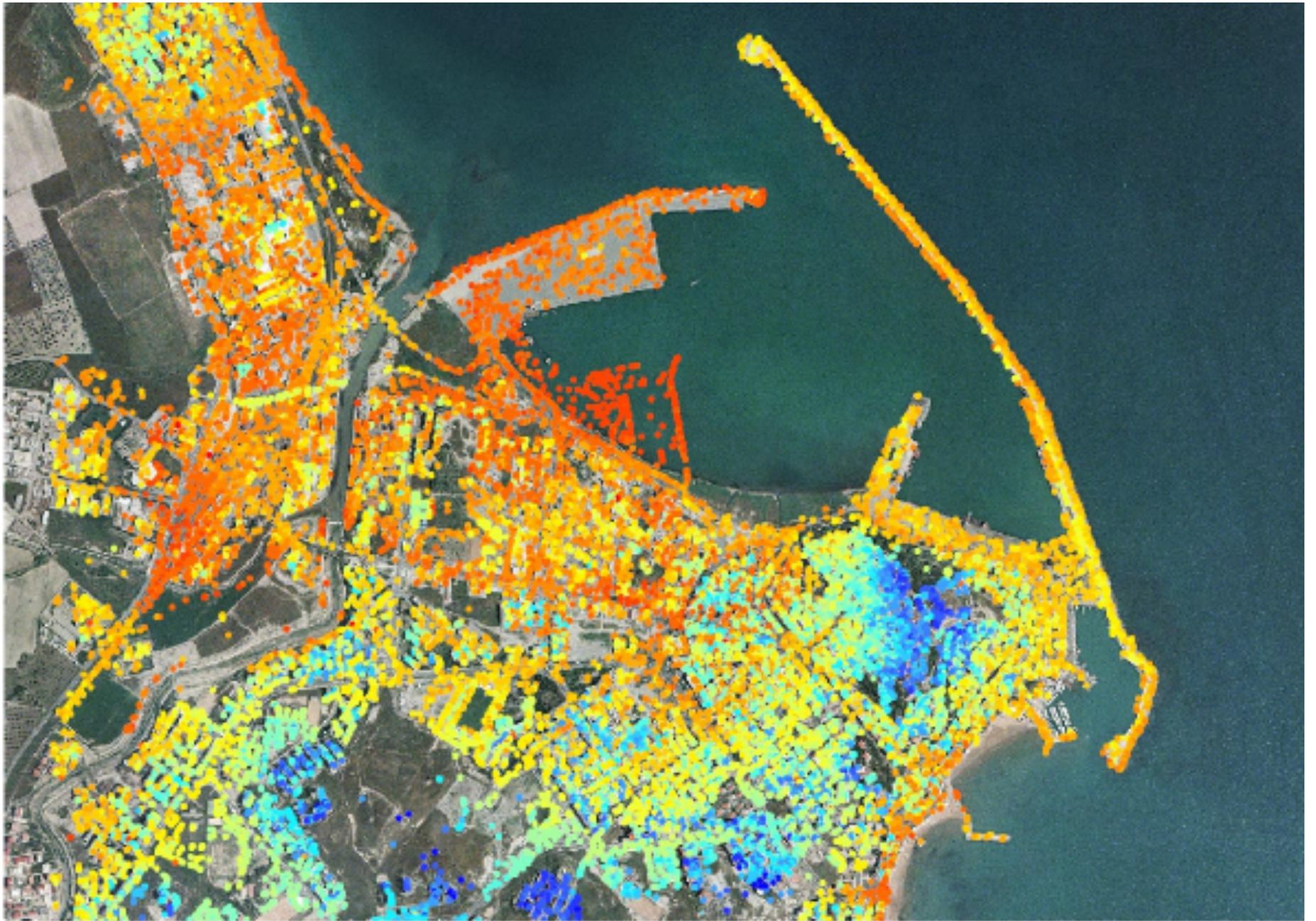




0 500 1.000 Meters

Number of Images: 22  
First Acquisition: 23 Dec 2006  
Last Acquisition: 07 Sep 2008

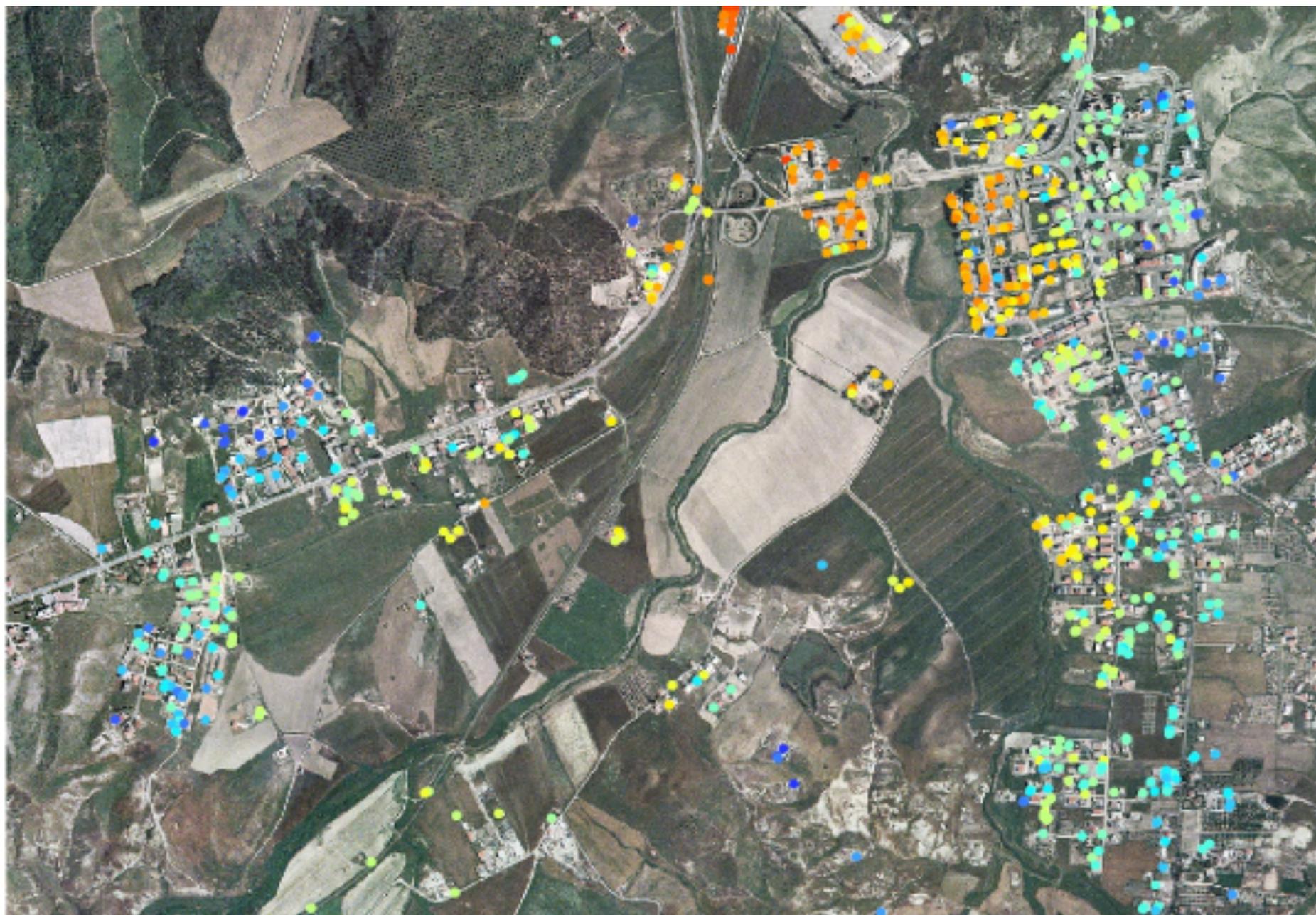
PSInSAR™ Analysis  
RSAT-1 Descending Data



0 500 1,000 Meters

Number of Images: 22  
First Acquisition: 25 Apr 2008  
Last Acquisition: 14 Jan 2009

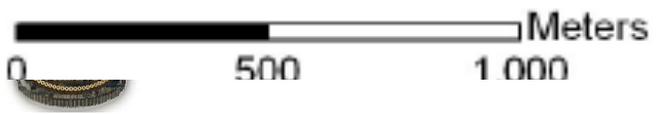
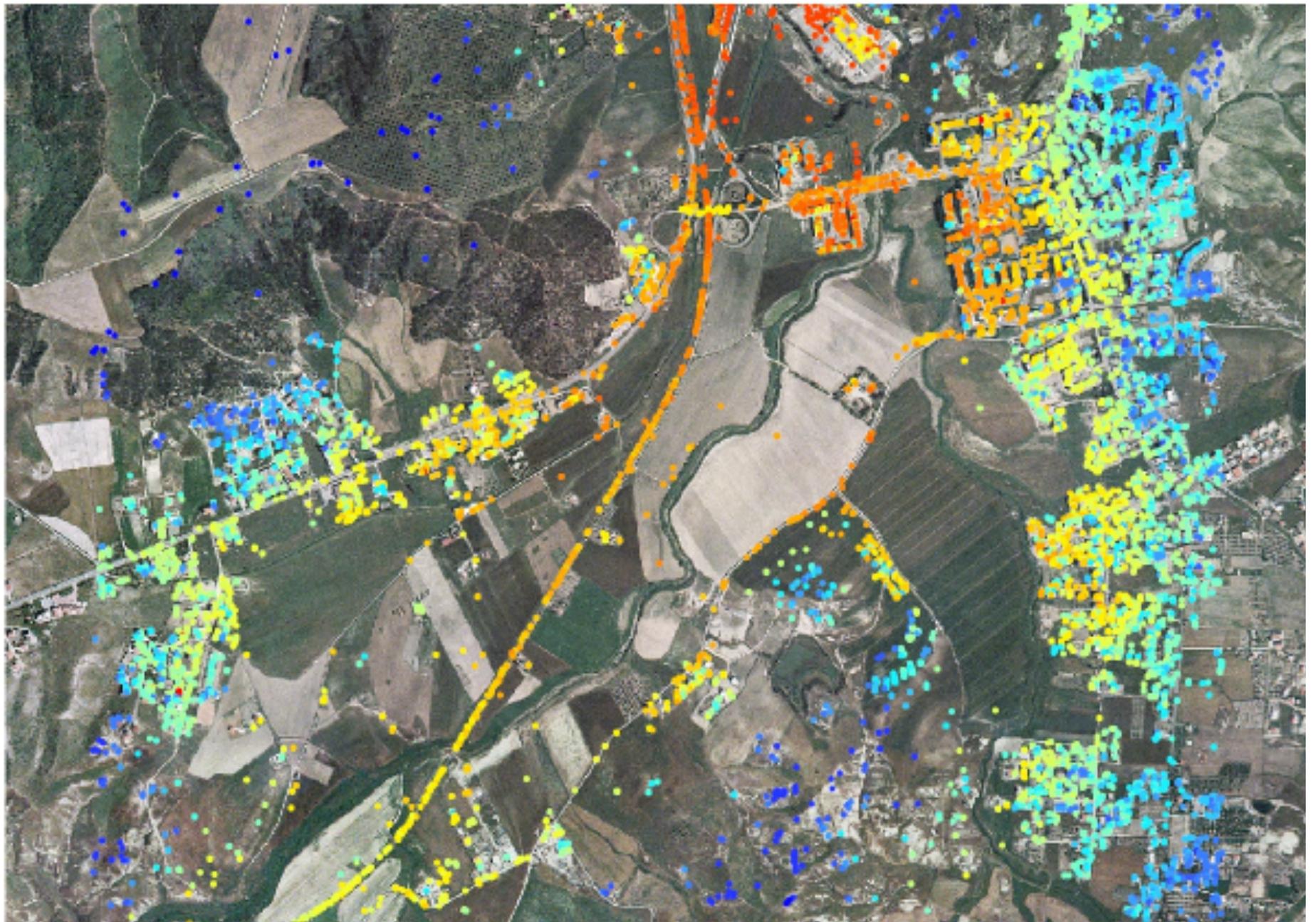
PSInSAR™ Analysis  
TerraSAR-X Descending Data  
TRE



0 500 1,000 Meters

Number of Images: 22  
First Acquisition: 23 Dec 2006  
Last Acquisition: 07 Sep 2008

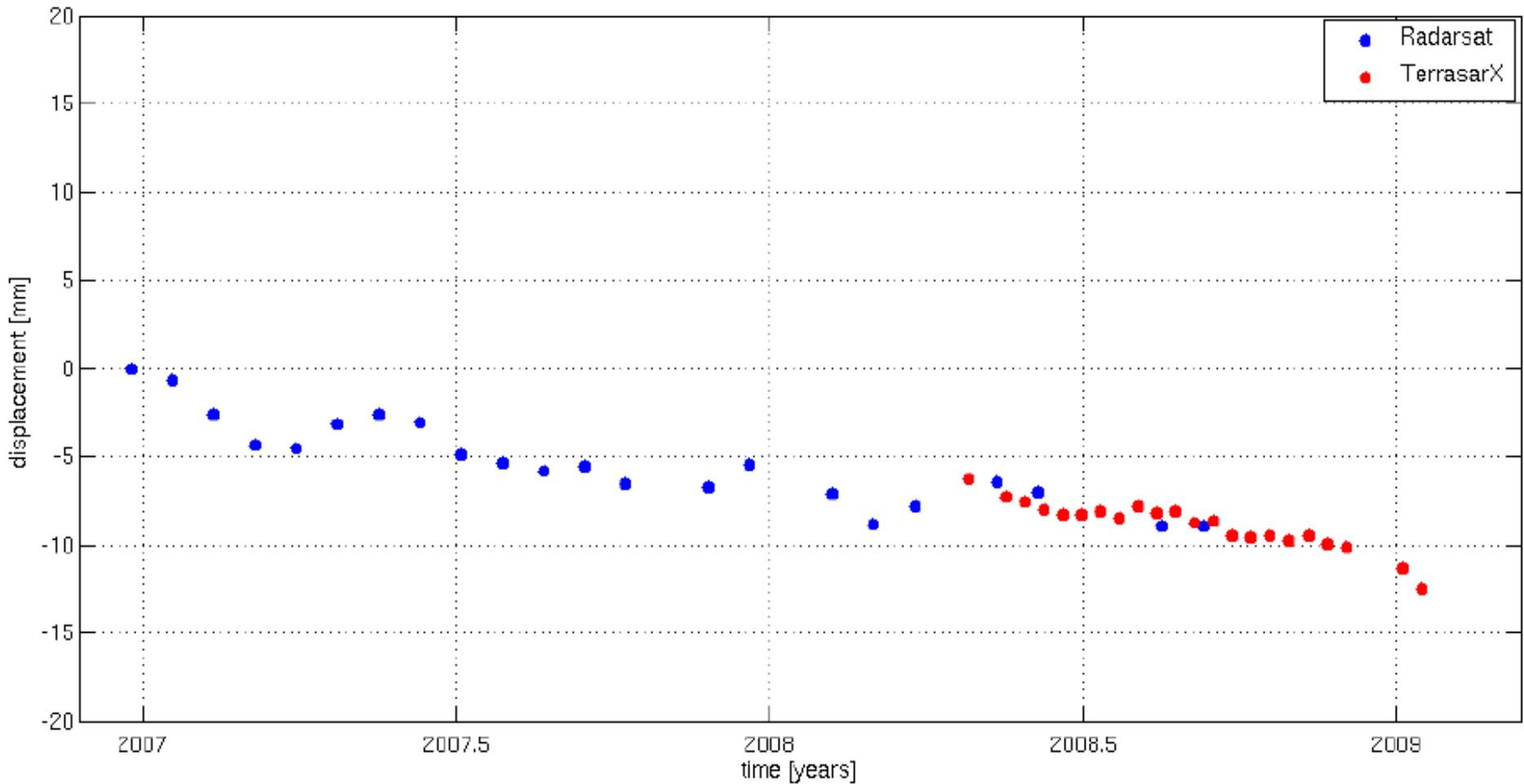
PSInSAR™ Analysis  
RSAT-1 Descending Data



Number of Images: 22  
First Acquisition: 25 Apr 2008  
Last Acquisition: 11 Jan 2009

PSInSAR™ Analysis  
TerraSAR-X Descending Data

We are close to the objective; the revisit time of Sentinel 1A/B it is 6 days



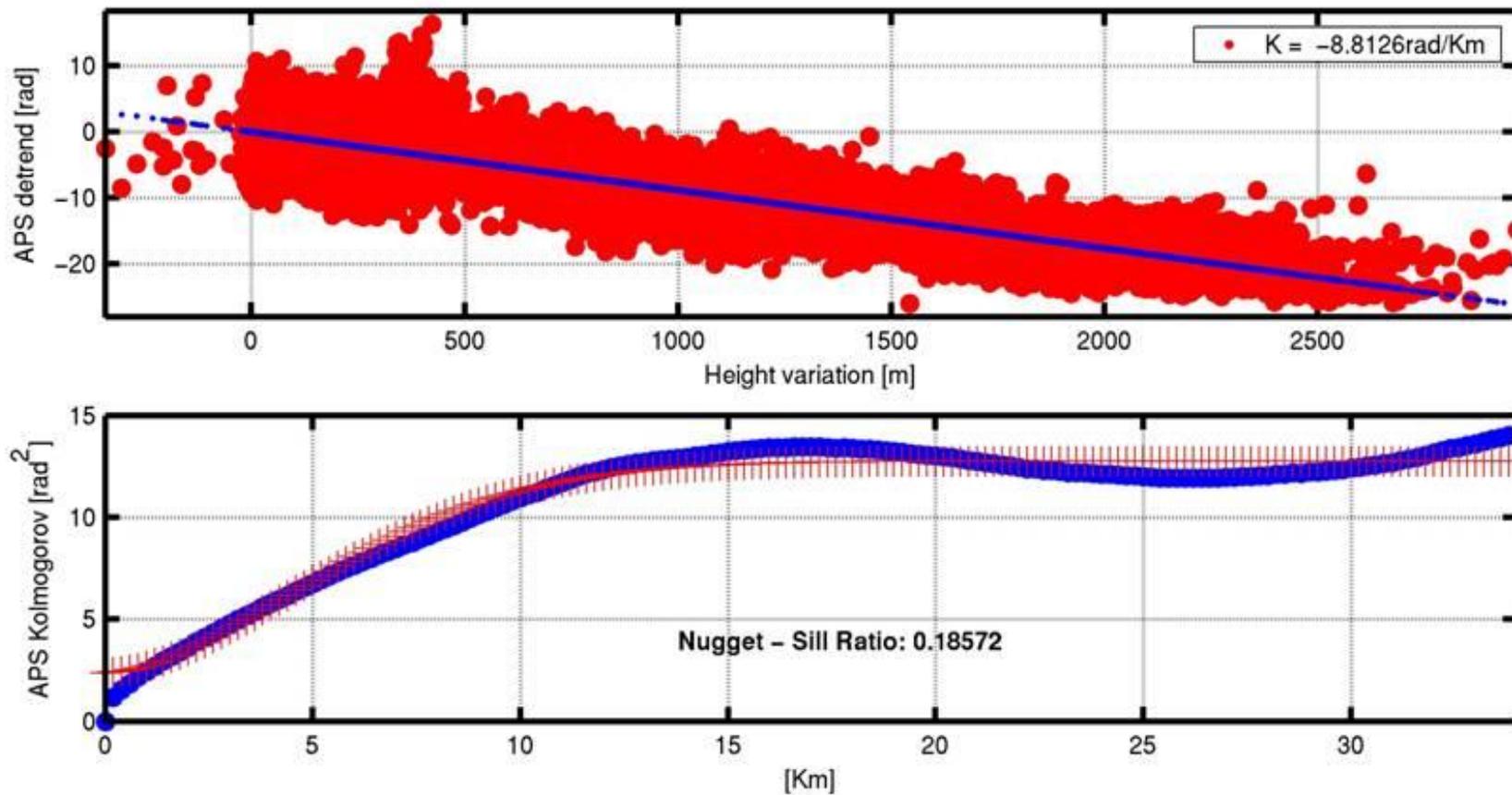
# Controlling the Atmospheric Phase Screen without a dense and long set of PS

Density Time series	Dense	Sparse
Long	OK	Distrib. Scatt. NWP
Short	NWP	UAV, Geo synchronous?

Today, Numerical Weather Predictions yield useful Water Vapor topographic gradients but not the turbulent component. This may improve with a better description of the Boundary Layer (towns, forest, etc). Besides, InSAR is instantaneous, NWP time smooth.  
TIGIR, 2009



## Statistics of atmospheric data



rms delay  $\approx 10\text{mm}$  two way

## Dense and **short** data sets

Using the APS estimates from NWP

Estimate the master of the  $N_i$  interferometric takes using the  $N_\psi$  estimates (GPS, MM5 etc.) and then remove it. The m.s. errors are:

$$\sigma_{\varepsilon,i}^2 = \frac{\sigma_a^2}{N_i}; \quad \sigma_{\varepsilon,NWP}^2 = \frac{\sigma_\psi^2}{N_\psi}; \quad k = \frac{\sigma_\psi^2}{\sigma_a^2}$$

The gain  $G$  (as if we had  $N_i'$  interferometric images) can be large if the NWP are good ( $k < 0.3$ ):

$$\frac{1}{\sigma_{\varepsilon,t}^2} = \frac{N_i'}{\sigma_a^2} = \frac{N_i}{\sigma_a^2} + \frac{N_\psi}{\sigma_\psi^2}$$

$$G = \frac{N_i'}{N_i} = 1 + \frac{N_\psi}{N_i} \frac{\sigma_a^2}{\sigma_\psi^2}$$



## Long and **sparse** data sets

If the revisit time is short, we can use distributed scatterers, that slowly decorrelate. For C band the decorrelation time constant is  $\tau \approx 40$  days. For 1 month,  $L$  looks,  $N=5$  revisits, the dispersion of the subsidence estimate due to decorrelation is

$$\sigma_{m,1mo} = \frac{\lambda}{4\pi} \sqrt{\frac{1-\gamma^2}{2LN\gamma^2}}$$

$$\gamma = \gamma_0 \exp(-T/\tau) = 0.6e^{-6/40} = 0.51$$

$$\sigma_{m,1mo} = 5.4 \sqrt{\frac{1}{NL}} \text{ mm / mo} = 0.24 \text{ mm / mo in } 100 \times 100 \text{ m}^2$$

Now, we have to consider the APS



# Interferogram stacking and subsidence

When the targets decorrelate, interferogram stacking is optimal. The resulting subsidence velocity dispersion is (C band, L looks):

$$\sigma_{s,decor,Tobs} = \frac{\lambda}{4\pi} \frac{T_{obs}}{T} \sqrt{\frac{T}{T_{obs}}} \sqrt{\frac{1-\gamma^2}{2\gamma^2}} = 42 \sqrt{\frac{1}{L}} \text{mm/year}$$

An atmospheric bubble,  $\emptyset = .8\text{km}$ , contains 5000 looks. Then,  $\sigma_{s,decor} \sim .6\text{mm/year}$ , lower than the effect of the APS  $\sim 1.3\text{mm}/\sqrt{M \text{ years}}$ .

We either need NWP or multiannual time series.



# Conclusions

For the oil and CO<sub>2</sub> applications, spatial resolution is not essential, but short revisit time and good vertical precision are paramount

With a dense and long set of PS (desert areas), we are already below the millimeter error.

In the case of **short** or **sparse** data sets, we need improved **Numerical Weather Predictions**.

*... Les nez ont été faits pour porter des lunettes  
Noses were made to hold glasses  
Voltaire, Candide*



The competition:  
Optical and GPS levelling:  
Approximate results



# A recent survey comparison for an accelerator design in Japan

The 10th International Workshop on Accelerator Alignment, KEK, Tsukuba, 11-15 February 2008

## **SURVEY COMPARISON USING GNSS AND ME5000 FOR ONE KILOMETER RANGE**

S.Matsui, H.Kimura, RIKEN, Kouto, Sayo-cho, Sayo-gun, Hyogo, 679-5148 JAPAN



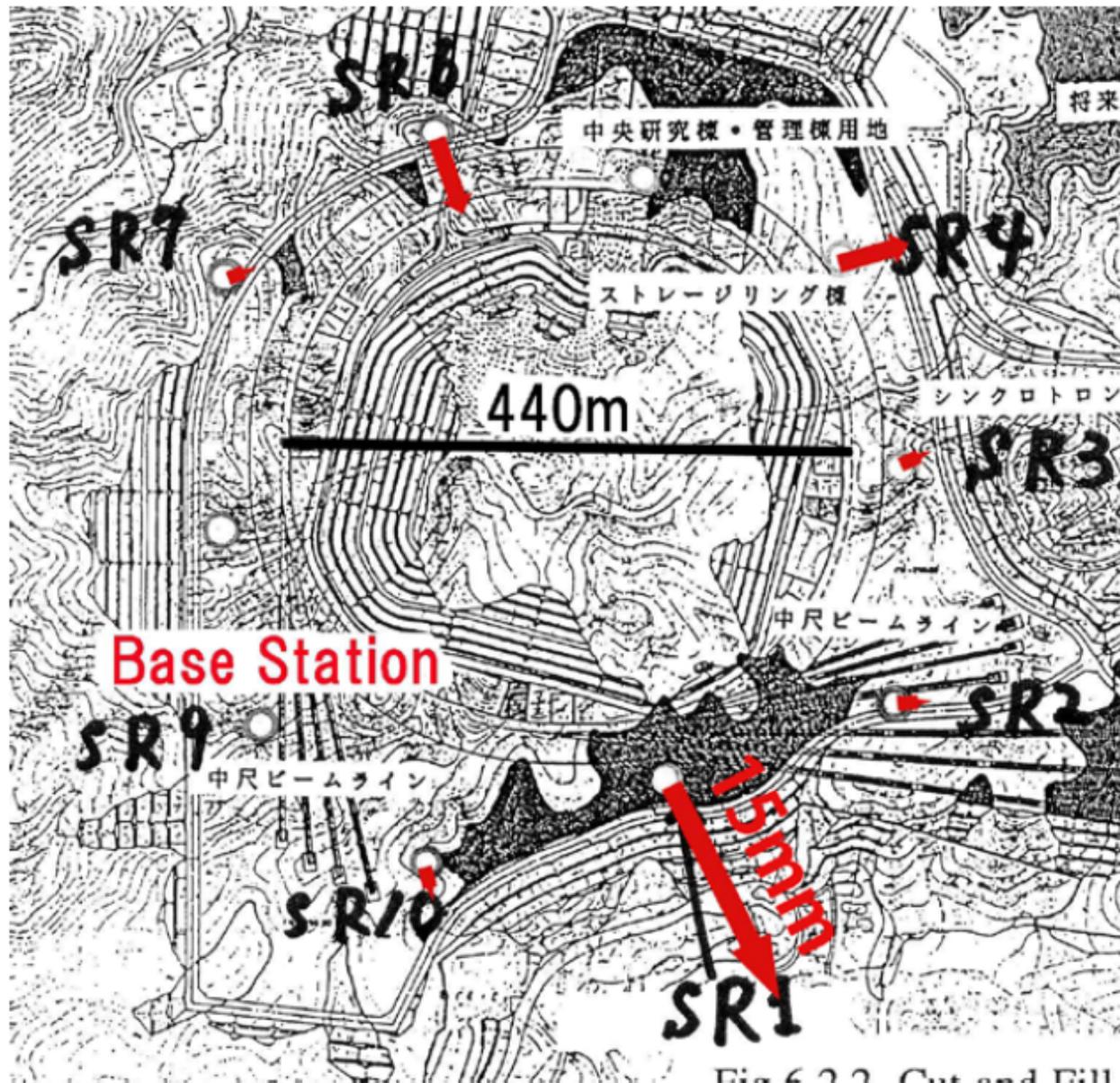


Fig. 6.2.2. Cut and Fill

Fig.22. Shifts of survey monuments for sixteen years.



# Error ellipse

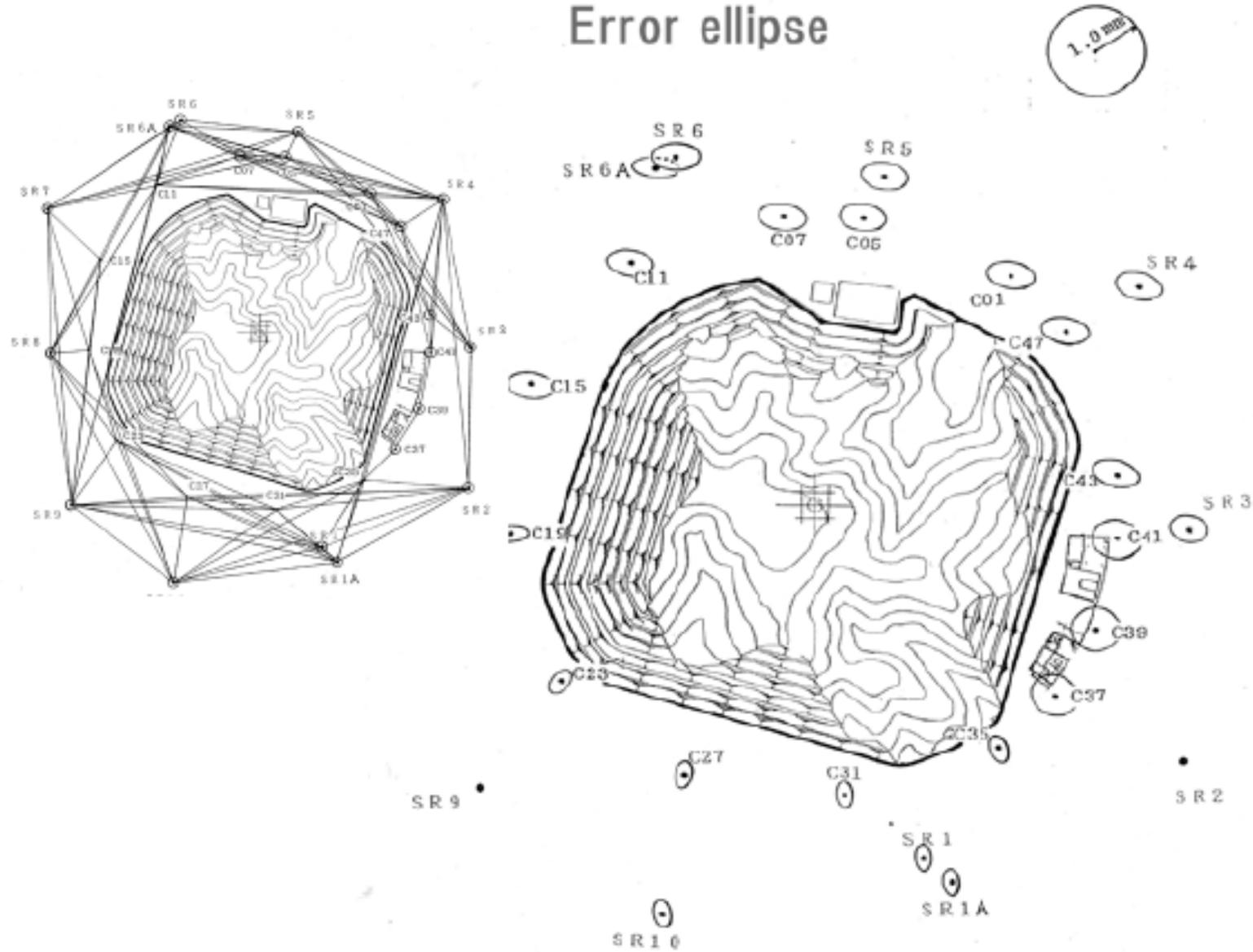


Fig.19. Survey network and error ellipses.



Fig. 6. Two GNSS antenna on the stage.

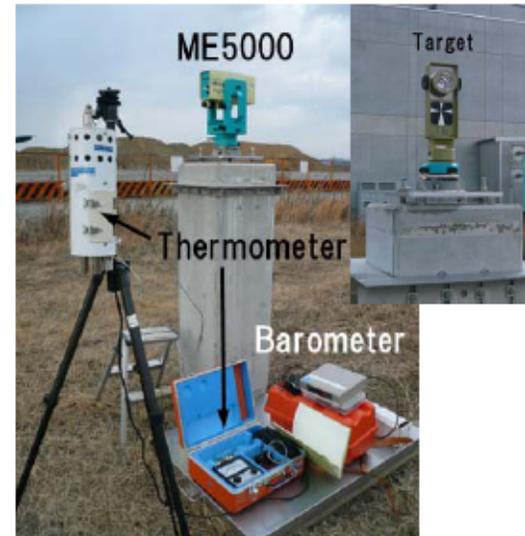


Fig.11. Mekometer, thermometer and barometer.

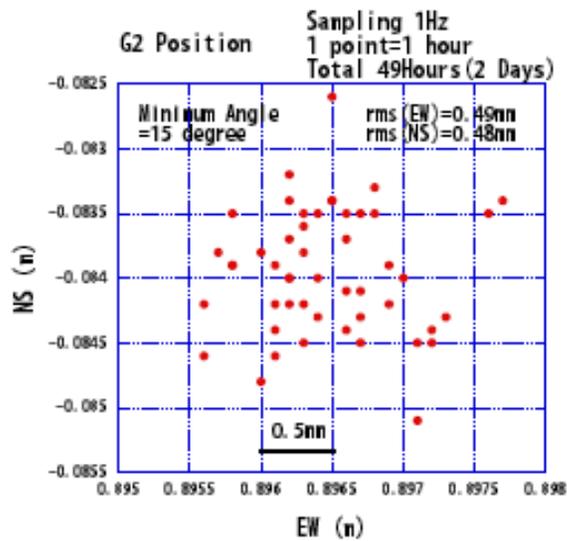


Fig.7. Fluctuation of the GNSS position result for 2 days.



Fig.13. One kilometer baseline and GNSS receivers in the SPring-8 site.



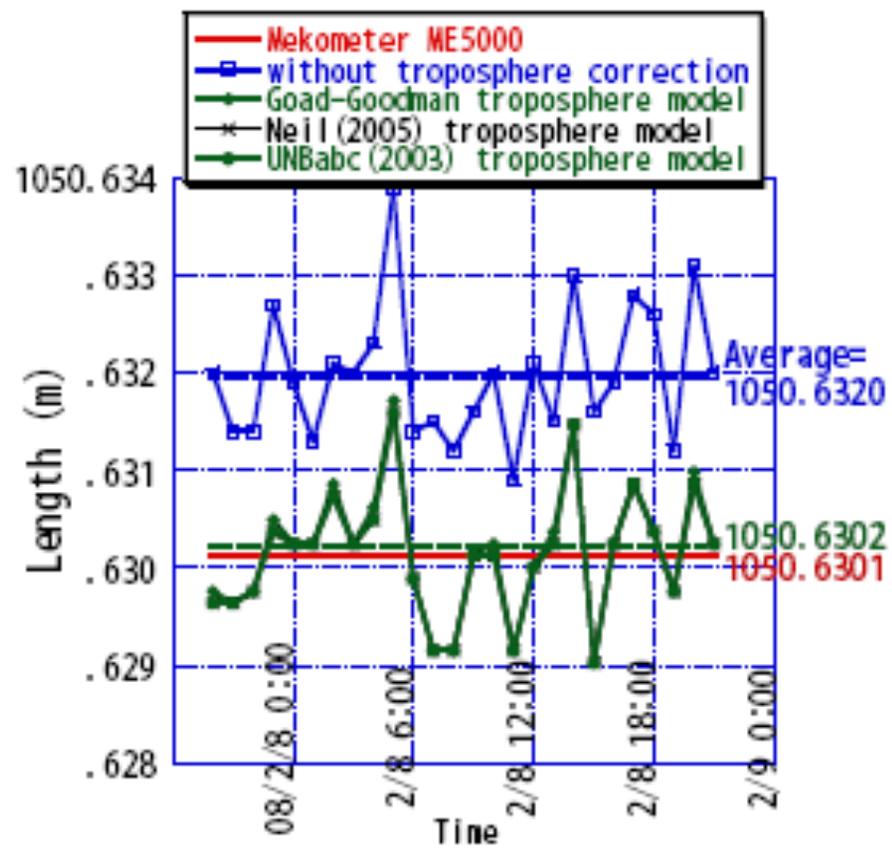


Fig.14. Distance comparison of one kilometer baseline between ME5000 and GNSS.

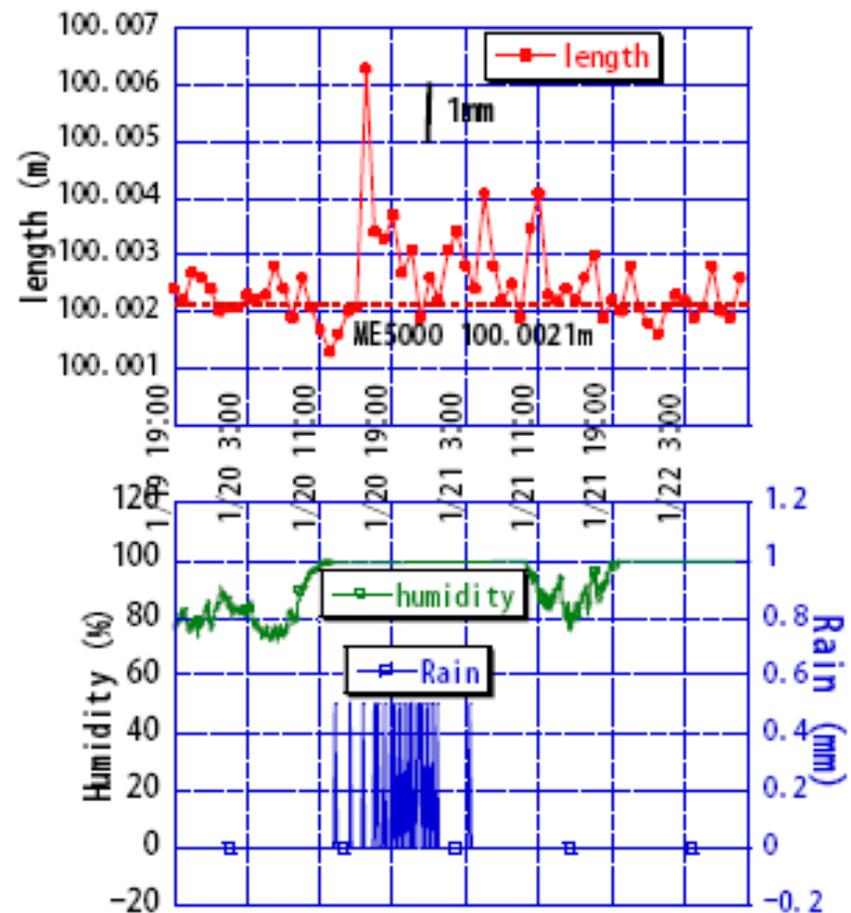


Fig.15. Distance and the influence of rain.



# The future: Photon counting devices

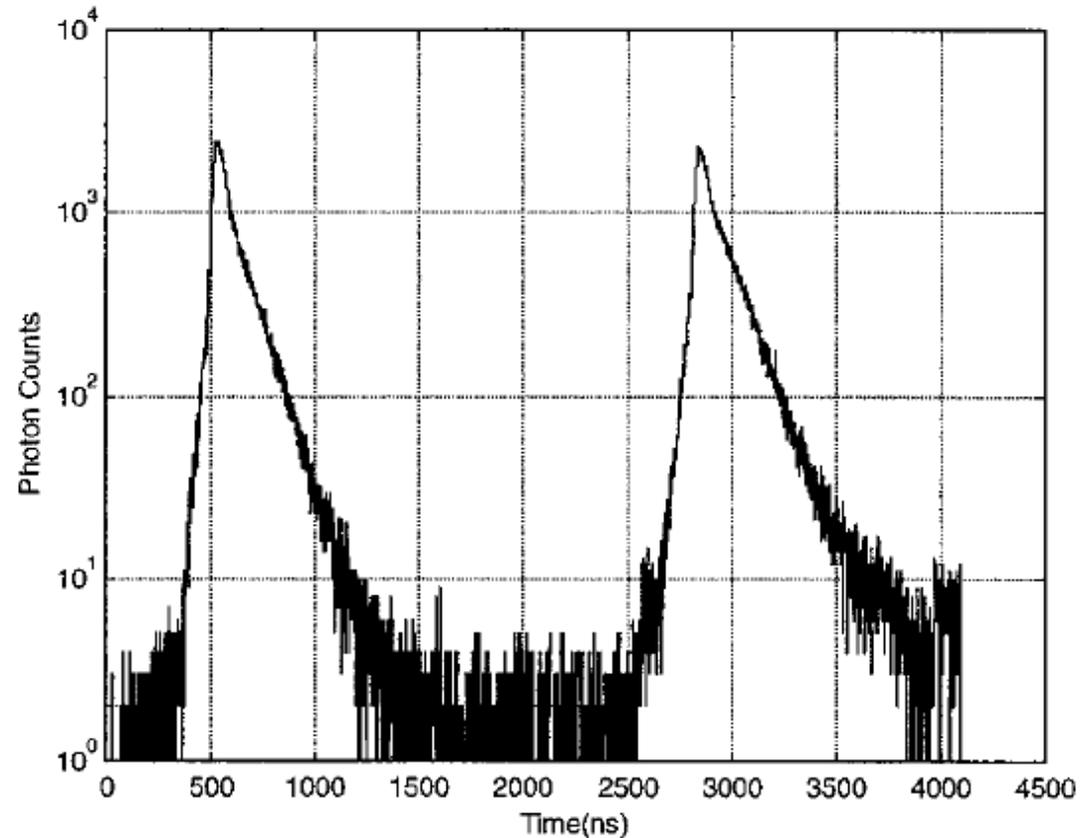


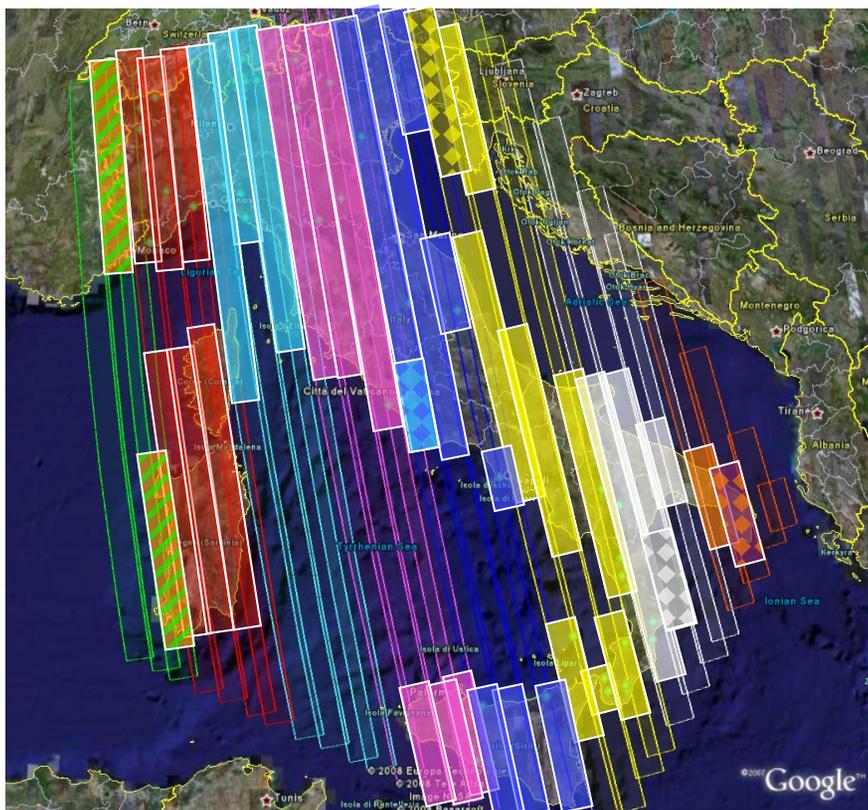
Fig. 3. Histogram of photon-count data. The target peak is on the left and the reference peak is on the right.

Photon-counting detector with an accuracy of 20 ps (3.3 mm two way)

*Max point rate ~ 1000 pts/sec*

*Low atmospheric effects*





*Cosmo SkyMed and variable revisit times.*

<i>Uniform:</i>	<i>16d;</i>
<i>checkerboard</i>	<i>8d;</i>
<i>stripes</i>	<i>4d.</i>

A constellation of  $N$  satellites with revisit time  $T$ , may dedicate  $N-1$  passages to one location, and the  $N$ -th passage to the entire strip, with a  $1/N$  azimuth resolution. trading revisit time and resolution,

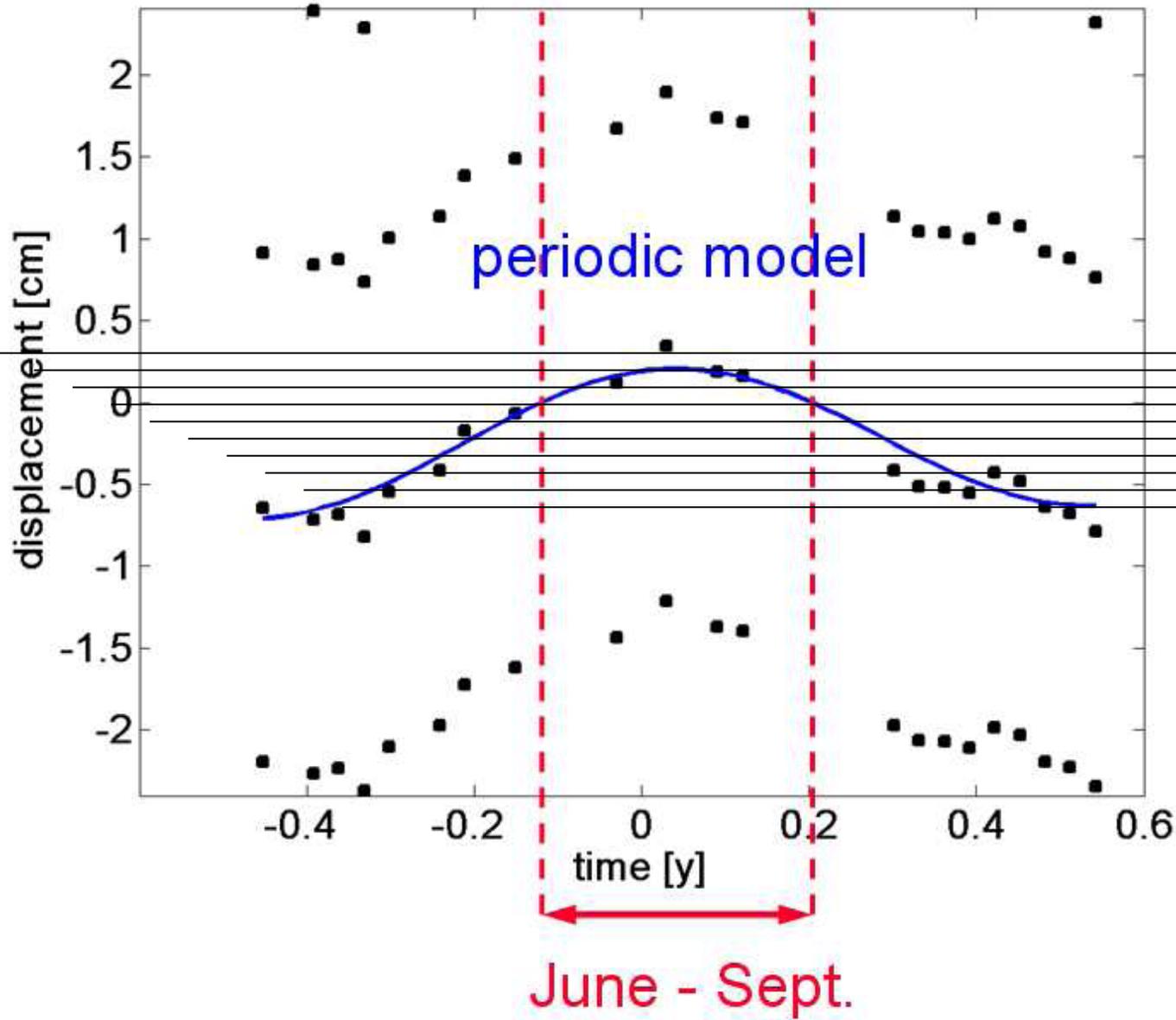


# Seafloor geodesy

Sonardyne - Shell deployed two 10 sensors sonar networks to measure to the cm underwater displacements at 1km (depth or horizontal motion).

The main problem are water velocity changes.





Terrasar X Berlin

